

Proof of Theorem 60

The theorem to be proved is

$$x \leq x$$

Suppose the theorem does not hold. Then, with the variables held fixed,

$$(H) \quad [[\neg (x) \leq (x)]]$$

Special cases of the hypothesis and previous results:

$$0: \quad \neg x \leq x \quad \text{from } H:x$$

$$1: \quad x \leq x \quad \vee \quad \neg x - x = 0 \quad \text{from } \underline{55}^{<};x;x$$

$$2: \quad x - x = 0 \quad \text{from } \underline{19};x$$

Inferences:

$$3: \quad \neg x - x = 0 \quad \text{by}$$

$$0: \quad \neg x \leq x$$

$$1: \quad x \leq x \quad \vee \quad \neg x - x = 0$$

$$4: \quad QEA \quad \text{by}$$

$$2: \quad x - x = 0$$

$$3: \quad \neg x - x = 0$$